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RESEARCH ARTICLE

Systems Biology Investigation of cAMP Modulation to Increase SMN Levels for the Treatment of Spinal Muscular Atrophy

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Abstract

Spinal muscular atrophy (SMA), a leading genetic cause of infant death worldwide, is an autosomal recessive disorder caused by the loss of SMN1 (survival motor neuron 1), which encodes the protein SMN. The loss of SMN1 causes a deficiency in SMN protein levels leading to motor neuron cell death in the anterior horn of the spinal cord. SMN2, however, can also produce some functional SMN to partially compensate for loss of SMN1 in SMA suggesting increasing transcription of SMN2 as a potential therapy to treat patients with SMA. A cAMP response element was identified on the SMN2 promoter, implicating cAMP activation as a step in the transcription of SMN2. Therefore, we investigated the effects of modulating the cAMP signaling cascade on SMN production in vitro and in silico. SMA patient fibroblasts were treated with the cAMP signaling modulators rolipram, salbutamol, dbcAMP, epinephrine and forskolin. All of the modulators tested were able to increase gem formation, a marker for SMN protein in the nucleus, in a dose-dependent manner. We then derived two possible mathematical models simulating the regulation of SMN2 expression by cAMP signaling. Both models fit well with our experimental data. In silico treatment of SMA fibroblasts simultaneously with two different cAMP modulators resulted in an additive increase in gem formation. This study shows how a systems biology approach can be used to develop potential therapeutic targets for treating SMA.
Introduction

Spinal muscular atrophy (SMA) is an autosomal recessive, neurodegenerative disorder characterized by the progressive loss of α-motor neurons in the anterior horn of the spinal cord; this loss leads to progressive muscle weakness and atrophy [1]. SMA is a leading genetic cause of infant death worldwide with 1 in 5000–10,000 children born with the disease [2, 3]. Loss of or mutation in SMN1 (survival motor neuron 1) leads to SMA [4]. In humans and only in humans, SMN1 is duplicated to yield SMN2 [5, 6]. There is a single nucleotide change (C→T) within SMN2 exon 7 that causes most of SMN2 mRNAs to lack exon 7 (SMNΔ7). The resultant SMNΔ7 protein is unstable and not fully functional [7, 8]. SMN2 can, however, provide some full-length, functional SMN (FL-SMN) protein. The number of SMN2 copies modifies disease severity in SMA patients [9–16]. In transgenic mouse models for SMA, the copy number of human SMN2 modulates the phenotypic severity [17–19]. SMN2 is, therefore, an endogenous genetic modifier of disease severity in SMA.

Because of this phenotype modifying property, SMN2 has been the target for numerous drug discovery strategies. Targeting cyclic adenosine monophosphate (cAMP) signaling is of particular interest in developing inducers of SMN2 expression. The cAMP signaling cascade (Fig. 1) is used by both prokaryotes and eukaryotes to regulate various processes including cell growth, metabolism and stress response [20]. The SMN2 promoter contains at least one cAMP-response element (CRE) that is able to bind to activated CRE-binding protein (phospho-CREB) [21]. The β2-adrenergic agonist salbutamol increases the amount of FL-SMN protein in SMA fibroblasts and leukocytes of SMA patients [22, 23]. Forskolin, which stimulates adenylyl cyclase (AC) catalysis to produce cAMP from ATP, increases SMN2 promoter activity [21]. The synthetic analogue dibutyryl cAMP (dbcAMP)—which activates cyclic AMP-dependent protein kinase (PKA)—also increases SMN2 promoter activity [21]. Taken together, these studies show that modulation of cAMP signaling can increase SMN expression from SMN2.

In this study, we will examine the effect of modulating cAMP signaling on SMN expression in SMA cells using a systems biology approach. cAMP signaling will be regulated by one of four possible targets (Fig. 1): activation of G protein-coupled receptors, activation of AC, activation of PKA and inhibition of phosphodiesterases (PDEs) that break down cAMP. Within the nuclei of most eukaryotic cells, SMN protein localizes to discreet foci known as gems, or gemini of coiled bodies [24]. The number of gems are markedly reduced within the nuclei of cells from SMA patients [9]. Using gem formation as an indicator of the expression of functional, FL-SMN protein, we will develop computational models of interactions between the cAMP pathway and gem formation to investigate how modulating cAMP signaling dynamics affects FL-SMN production. This systems biology approach consists of a synergistic interaction between experimental data and mathematical models. The experimental data and domain knowledge are used to develop the initial models and through a process of iteration, the model
assumptions are updated to come up with an improved model [25]. Such a systems modeling approach can ultimately aid in the development and optimization of cAMP signaling-based therapeutic strategies for SMA.

**Materials and Methods**

**Fibroblast Cell Culture**

GM03813 fibroblasts [26] (Coriell Cell Repositories; Camden, NJ) were derived from a SMA patient with deletion of SMN1 and 2 copies of SMN2. GM03814 fibroblasts [26] (Coriell Cell Repositories) were derived from the carrier mother of GM03813; this line, therefore, carries 1 copy of SMN1. All fibroblast lines were maintained in Dulbecco’s modified essential medium (DMEM; Life Technologies, Grand Island, NY) containing 10% fetal bovine serum (FBS; Atlas Biologicals, Fort Collins, CO), 2 mM L-glutamine (Life Technologies) and 1% penicillin/streptomycin (Life Technologies).

**Drug Treatment**

Cells were seeded onto gelatinized glass coverslips at a density of 4000 cells/cm². Cells were treated with one of the following compounds (n=3/dose): dbcAMP (5–
500 μM; EMD Millipore, Billerica, MA), epinephrine (1–100 nM; Sigma-Aldrich, St. Louis, MO), forskolin (0.5–50 μM; EMD Millipore), salbutamol (1–100 nM; Sigma-Aldrich), rolipram (0.1–10 μM; Sigma-Aldrich) or vehicle. ddH2O was utilized as the vehicle for the dbcAMP treatments while DMSO was the vehicle for the remaining compounds. Test compounds were added to the medium at a 1:1000 dilution. Medium was changed daily and fresh compound was added for 5 days.

Immunofluorescence
Immunostaining of fibroblast cells was accomplished as described previously [27]. Briefly, cells grown on gelatinized coverslips were fixed with Fixative Buffer (2% paraformaldehyde, 400 μM CaCl2, 50 mM sucrose in 100 mM sodium phosphate buffer, pH 7.4) for 30 min at room temperature, thoroughly rinsed with phosphate-buffered saline (PBS) and permeabilized with ice-cold acetone for 10 min. After drying for at least 30 min at room temperature, the cells were rehydrated with PBS for 10 min at room temperature and then blocked with 5 x BLOCK for 60 min at room temperature. The cells were incubated overnight with primary antibody solution (mouse anti-SMN mAb (MANSMA2 (8F7); Developmental Studies Hybridoma Bank, Iowa City, IA [28]) diluted 1:200 in 1 x BLOCK) at 4 °C. The cells were then washed extensively (3 x 10 min) with PBS and incubated with secondary antibody solution (biotinylated goat anti-mouse IgG (Jackson ImmunoResearch) diluted 1:400 with 1 x BLOCK) for 60 min at room temperature. The cells were then washed with PBS (3 x 10 min) and then incubated with AlexaFluor 594-conjugated streptavidin (Life Technologies) diluted 1:200 with PBS for 60 min at room temperature. Cells were then counterstained with Hoescht 33342 (1 μg/mL; Life Technologies) in PBS for 5 min. After thorough washing with PBS, coverslips were mounted onto glass slides with ImmuMount (Shandon Lipshaw) and stored at 4 °C until analysis.

Gem Count Analysis
SMN immunostaining in fibroblasts was visualized using a DMRXA2 epifluorescence microscope (Leica Microsystems) with an ORCA-ER cooled camera (Hamamatsu, Hamamatsu City, Japan) and Volocity 6.1.1 software (PerkinElmer). For gem counting, the following parameters were measured in 100 randomly selected nuclei: the number of gems, the number of cells with gems and the number of cells with more than 1 gem. The gem counts were converted into a concentration value (in mM) using an approximate average cell volume (2.68 x 10^{-13} L). This conversion assumes that all cells are of equal volume [29].

Development of Mathematical Models
The computational model was visualized and developed in CellDesigner [30]. Each model was then converted into Systems Biology Markup Language (SBML)
format [31] and imported into MATLAB using SBToolbox [32]. SBToolbox was used to complete parameter sensitivity and model simulations.

Simplified cAMP Model

Model Derivation

In order to adapt the Williamson model [33] to our system, their parameters required reworking to be in accordance with the units of our data. The Williamson model was shown to match data from literature [34, 35] which is reported in units of nmol per gram wet weight versus minutes. Through careful inspection, the time units of the model were determined to be 20 seconds (s) (i.e. one time unit represents 20 s in the data) with the concentration units remaining the same as the data. The data points of the model results presented in Williamson were extracted using WebPlotDigitizer v.2.6 (http://arohatgi.info/WebPlotDigitizer) and converted into the proper units.

Our simplified model consists of three ordinary differential equations (ODEs; Equations 1–3) and two conservation equations (Equations 4 & 5). Equation 1 represents the rate of change in the active form of the G protein receptor (GP_a) in the presence or absence of a stimulatory hormone or agonist. Equation 2 models the instantaneous changes in active PKA (PKA_a) as a result of cAMP production. Equation 3 captures both cAMP production from ATP by AC and degradation into AMP via PKA_a-stimulated PDE activity. The conservation equations demonstrate the balance between the active and inactive forms of both GP and PKA.

In order to further simplify the system, the two PDE terms from the Williamson et al. model [33] were combined into one term. As evinced in the Williamson et al. study [33], PDE2 does not have a significant effect on cAMP concentration, especially when compared to PDE1. Since there are multiple isoforms of PDEs in humans [36], we generated a general PDE term to model the overall inhibitory action of PDEs in the cells. The model parameters were defined as in [33] and their descriptions are summarized in Table 1.

\[
\frac{d[GP_a]}{dt} = k_f ([totalGP] - [GP_a][Hormone] - k_r [GP_a]) \quad (1)
\]

\[
\frac{d[PKA_a]}{dt} = k_f ([totalPKA] - [PKA_a][cAMP] - k_r [PKA_a]) \quad (2)
\]

\[
\frac{d[cAMP]}{dt} = \frac{AC_{basal} + k_A[GP_a]}{1 + K_i[PKA_a]} \cdot \frac{[PKA_a]V_{maxPDE}[cAMP]}{K_MPDE + [cAMP]} \quad (3)
\]

\[
[totalGP] = [GP_a] + [GP_i] \quad (4)
\]
The model was then fit to the converted experimental data using the optimization algorithms detailed below. The optimized parameters determined from this model fitting are listed in Table 1.

The experimental data utilized by Williamson et al. [33] represented concentration in units of nmol per gram wet weight (gww). However, the glucose pulse used in this study was in units of mM. In order to convert the data into mM concentrations, the following equation was used:

\[
C(nM) = \frac{c(nmol/gww)c_w}{(1000nmol/mmol)V_c}
\]

where \(C(nM)\) is concentration of cAMP in milimolar, \(c_w\) is the conversion factor to grams dry weight (0.15) and \(V_c\) is the volume of \(10^7\) cells (2.68 \(\times\) \(10^{-6}\) L; approximately \(10^7\) cells in 1 gww). The equation and constant values were adapted from the equation detailed in Williamson et al. [33].

---

Table 1. Optimized parameter values for cAMP pathway full cAMP:SMN2 model.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
<th>Units</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>GP ( k_f )</td>
<td>G-Protein Activation Rate</td>
<td>(1.33 \times 10^{-7})</td>
<td>(mM/min)(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>GP ( k_r )</td>
<td>G-Protein Deactivation Rate</td>
<td>(2.05 \times 10^{-7})</td>
<td>min(^{-1})</td>
<td>This Work*</td>
</tr>
<tr>
<td>PKA ( k_f )</td>
<td>PKA Activation Rate</td>
<td>5.37</td>
<td>(mM/min)(^{-1})</td>
<td>This Work*</td>
</tr>
<tr>
<td>PKA ( k_r )</td>
<td>PKA Deactivation Rate</td>
<td>0.65</td>
<td>min(^{-1})</td>
<td>This Work*</td>
</tr>
<tr>
<td>( AC_{basal} )</td>
<td>Base AC Activation Rate</td>
<td>(1.00 \times 10^{-5})</td>
<td>mM/min</td>
<td>This Work*</td>
</tr>
<tr>
<td>GP ( k_a )</td>
<td>G-Protein Catalysis Rate</td>
<td>87.83</td>
<td>min(^{-1})</td>
<td>This Work*</td>
</tr>
<tr>
<td>PKA ( K_i )</td>
<td>PKA Inhibition Rate</td>
<td>1419.09</td>
<td>mM(^{-1})</td>
<td>This Work*</td>
</tr>
<tr>
<td>( V_{max,PDE} )</td>
<td>Max cAMP Degradation Rate</td>
<td>1.75</td>
<td>min(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( K_{PDE} )</td>
<td>PDE Dissociation Rate Constant</td>
<td>7.79</td>
<td>mM</td>
<td>This Work</td>
</tr>
<tr>
<td>CREB ( k_f )</td>
<td>CREB Phosphorylation Rate</td>
<td>59.54</td>
<td>(mM/min)(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>CREB ( k_r )</td>
<td>CREB De-phosphorylation Rate</td>
<td>0.93</td>
<td>min(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( k_{max} )</td>
<td>Max Transcription Rate</td>
<td>(1.14 \times 10^{-5})</td>
<td>mM/min</td>
<td>This Work</td>
</tr>
<tr>
<td>( c )</td>
<td>Promoter Binding Efficiency</td>
<td>(8.61 \times 10^{-3})</td>
<td>mM(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( d_m )</td>
<td>mRNA Degradation Rate Constant</td>
<td>(2.10 \times 10^{-3})</td>
<td>min(^{-1})</td>
<td>[56]</td>
</tr>
<tr>
<td>( H )</td>
<td>Hill Coefficient</td>
<td>1</td>
<td>n/a</td>
<td>This Work</td>
</tr>
<tr>
<td>( k_p )</td>
<td>Translation Rate Constant</td>
<td>9109.61</td>
<td>min(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( d_p )</td>
<td>FL-SMN Degradation Rate Constant</td>
<td>(2.70 \times 10^{-3})</td>
<td>min(^{-1})</td>
<td>[39]</td>
</tr>
<tr>
<td>( k_g )</td>
<td>Gem Formation Rate Constant</td>
<td>(3.07 \times 10^{-6})</td>
<td>min(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( d_g )</td>
<td>Gem Degradation Rate Constant</td>
<td>(7.70 \times 10^{-4})</td>
<td>min(^{-1})</td>
<td>[39]</td>
</tr>
<tr>
<td>( F_{Ka} )</td>
<td>Forskolin Catalysis Rate Constant</td>
<td>0.027</td>
<td>min(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>Salbutamol Splicing Constant</td>
<td>7172.40</td>
<td>mM(^{-1})</td>
<td>This Work</td>
</tr>
<tr>
<td>( K_i )</td>
<td>Rolipram Inhibition Constant</td>
<td>(1.71 \times 10^{-5})</td>
<td>mM</td>
<td>This Work</td>
</tr>
</tbody>
</table>

The parameters marked with an asterisk (*) were carried over from the simplified cAMP model.

\[ [totalPKA] = [PKA_a] + [PKA_i] \]  

The model was then fit to the converted experimental data using the optimization algorithms detailed below. The optimized parameters determined from this model fitting are listed in Table 1.
Parameter estimation

Parameters for the base model were estimated by fitting our modified model to the data extracted from the Williamson results through a simulated annealing algorithm \cite{37,38}, which is efficient at finding the global minimum for optimization. The algorithms were taken from Systems Biology Toolbox (SBToolbox) \cite{32} in MATLAB and the estimation was run using the SBparameterestimation function from SBToolbox as well as the main estimation functions listed in additional files.

Full cAMP:SMN2 Model

Model Development

In order to capture the treatment pathway of interest, the downstream effectors of the base model were incorporated to develop a model of how the cAMP pathway affects FL-SMN protein production and gem formation. Our full cAMP pathway model encompasses the base model equations with four additional ODEs (Equations 7–10) and one additional conservation equation (Equation 11). ODEs were derived for CREB phosphorylation by PKA\(_a\) (Equation 7), SMN2 promotion by phospho-CREB (Equation 8), translation of FL-SMN mRNA into FL-SMN protein (Equation 9) and the self-assembly of FL-SMN into gems (Equation 10). SMN2 activation was modeled using the Hill equation while the rest of the parameters were based on mass action kinetics. The conservation relationship detailed in Equation 11 represents the total CREB molecules in the cell. Each model parameter is defined in Table 1. Our model used units of min for time and mM for concentration.

\[
\frac{d[CREB_p]}{dt} = k_f([\text{total CREB}] - [CREB_p])[PKA_a] - k_r[CREB_p]
\]  

\[
\frac{d[SMN2mRNA]}{dt} = \frac{k_{max}(c[CREB_p])^H}{1 + (c[CREB_p])^H} - d_m[SMN2mRNA] - k_p[SMN2mRNA]
\]  

\[
\frac{d[FLSMN]}{dt} = k_p[SMN2mRNA] - k_g[FLSMN] - d_p[FLSMN]
\]  

\[
\frac{d[Gem]}{dt} = k_g[FLSMN] - d_g[Gem]
\]  

\[
[\text{total CREB}] = [CREB_p] + [CREB]
\]
Both salbutamol and epinephrine directly activate G proteins by binding with their receptors outside the cell. In our model, both compounds were directly substituted for the hormone concentration term in Equation 1:

$$[\text{Hormone}] = [\text{Salbutamol}] = [\text{Epinephrine}]$$  \hspace{1cm} (12)

In addition to activating the SMN2 promoter, salbutamol also alters the splicing of SMN2 mRNA causing an increase in FL-SMN production over SMN-D[22]. The interaction of salbutamol with the splicing machinery was modeled as proportional increase in the transcription rate of SMN2 mRNA given in Equation 8:

$$\text{Transcription rate} = \frac{k_{\text{max}}\left(1 + z \frac{[\text{Salbutamol}]}{C_{138}}\right)^H}{1 + \left(c \frac{[\text{CREB}_p]}{C_{138}}\right)^H}$$  \hspace{1cm} (13)

Treatments with the AC activator forskolin were modeled as an increase in basal AC activity proportional to the dosage of forskolin:

$$AC_{\text{basal}}^* = AC_{\text{basal}} + Fk_a[\text{Forskolin}]$$  \hspace{1cm} (14)

For the treatments with dbcAMP, the dose concentration was added directly to the existing cAMP concentration in the system:

$$[cAMP^*] = [cAMP] + [\text{dbcAMP}]$$  \hspace{1cm} (15)

Rolipram is a well-known PDE inhibitor, which indirectly causes an increase in cAMP. The inhibition interaction was modeled as reversible and competitive in Michaelis-Menten kinetics. The presence of the inhibitor alters the apparent Michaelis constant for the binding of cAMP to PDE:

$$K_M^{\text{app}, \text{PDE}} = K_M^{\text{PDE}}(1 + \frac{[R]}{K_i})$$  \hspace{1cm} (16)

where $[R]$ represents the concentration of rolipram and $K_i$ represents the inhibitor dissociation constant.

**Parameter Estimation**

Since the gem count data was collected after a treatment window of 5 days, the concentrations were treated as steady state values for the system. The steady state assumption allowed the model equations to be set to zero and solved for their constituent model states giving a system of algebraic equations. Due to the highly conserved nature of the cAMP pathway, the parameter values derived from the base model were carried over in order to reduce the parameter space to be optimized. A system of equations was derived through the steady state assumption on the full cAMP:SMN2 model.
The full cAMP:SMN2 model equations were solved for their principal model states (Equations 17–23). To eliminate the inter-dependence of cAMP and PKA, the cAMP variable was solved to give an equation for cAMP in terms of PKA (Equation 18) where Y represents the numerator of the AC term. This equation was then substituted into Equation 19 and solved for PKA using the equation solver in MATLAB (S1 Document).

\[
[GP_a^{ss}] = \frac{k_f ([S] + [E]) [GP_p]}{k_r + k_f ([S] + [E])}
\]  

Equation 17

\[
[cAMP^{ss}] = \frac{YK^{app}_m}{K_r V_m PDE [PKA_a^{ss}] + V_m PDE [PKA_a^{ss}] - Y}
\]  

Equation 18

\[
[PKA_a^{ss}] = \frac{k_f [cAMP^{ss}]}{k_r + k_f [cAMP^{ss}]} [PKA_t]
\]  

Equation 19

\[
[CREB_p^{ss}] = \frac{k_f [PKA_a^{ss}]}{k_r + k_f [PKA_a^{ss}]} [CREB_t]
\]  

Equation 20

\[
[SMN2mRNA^{ss}] = \frac{k_{max} (1 + \alpha [Salbutamol]) (c[CREB_p^{ss}])^H}{(d_m + k_p)(1 + (c[CREB_p^{ss}])^H)}
\]  

Equation 21

\[
[FLSMN^{ss}] = \frac{k_p}{k_g + d_p} [SMN2mRNA^{ss}]
\]  

Equation 22

\[
[Gem^{ss}] = \frac{k_g}{d_g} [FLSMN^{ss}]
\]  

Equation 23

Parameter estimation was completed through a sign squared error (SSE) analysis between the gem steady state concentrations derived from the gem count data and the full cAMP:SMN2 model calculations for each compound and dose. The parameter space was covered by generating a multidimensional matrix encompassing the possible combinations of parameter values over a specified range for each parameter to be estimated. For an easier model fit, the two controls were assumed to be identical and their data was averaged together.
Alternate cAMP:SMN2 Model

Model Development
An alternate pathway has been suggested in the literature [39] which shows active PKA directly stimulating the self-assembly of SMN into gems. Gems are much more stable than monomeric SMN so increasing the gem formation rate would increase the overall SMN concentration over time. Burnett et al. also found no noticeable increase in SMN mRNA levels coinciding with increased PKA_a levels suggesting that transcription is not involved. In order to examine the implications of the alternate pathway, a new model was developed by modifying our full cAMP:SMN2 model.

Equations 1, 2 and 3 from the full cAMP:SMN2 model were also used for this model. The key modifications made were the elimination of the CREB and transcription terms, simplification of translation to a constant rate, T, and the addition of PKA_a concentration to the gem formation term. The elimination of the CREB term also allowed for removal of the related conservation equation form the model. The alternate cAMP:SMN2 model parameters are defined in Table 3.

\[
\frac{d[FLSMN]}{dt} = T - k_g[PKA_a][FLSMN] - d_p[FLSMN]
\]

(24)

\[
\frac{d[Gem]}{dt} = k_g[PKA_a][FLSMN] - d_g[Gem]
\]

(25)

\[
[totalGP] = [GP_a] + [GP_i]
\]

(26)

\[
[totalPKA] = [PKA_a] + [PKA_i]
\]

(27)

The modifications made for each of the compounds were identical to the full cAMP:SMN2 model, except that the effect of salbutamol on splicing was represented as a proportional increase in the translation rate (Equation 28):

\[
T^* = T(1 + \alpha[Salbutamol])
\]

(28)

Parameter Estimation
Parameter optimization for the alternate cAMP:SMN2 model was completed using the steady state SSE analysis described earlier. The G protein, cAMP and PKA steady state equations were carried over from the full cAMP:SMN2 model and the FL-SMN (Equation 29) and gem (Equation 30) state equations were derived accordingly.

\[
[FLSMN^{ss}] = \frac{T(1 + \alpha[Salbutamol])}{k_g[PKA_a^{ss}] + d_p}
\]

(29)
Sensitivity Analysis

Steady state sensitivity analysis was completed according to the following equation:

\[
S_{nij} = \frac{X_{ss}(p_j + \Delta p_j) - X_{ss}(p_j)}{\Delta p_j} \times \frac{p_j}{X_{ss}(p_j)}
\]  

where \(S_{nij}\) is the normalized sensitivity of species \(i\) with respect to parameter \(j\), \(X_{ss}\) is species \(i\) at steady state, \(p_j\) is parameter \(j\), and \(\Delta p_j\) is the change in parameter \(j\). The sensitivities of gem concentration and FL-SMN concentration to changes in each of the system parameters were calculated.
Statistical Analysis
All quantitative data were expressed as mean ± standard error. Comparisons made between quantitative data were made using one-way ANOVA with a Bonferroni post hoc test. A p-value less than or equal to 0.05 was considered statistically significant. Statistical analyses of quantitative data were completed using SPSS v.22.

Results
Effect of Modulating cAMP Signaling on Gem Localization in SMA Fibroblasts
Fibroblasts derived from a type II SMA patient (GM03813; [26]) were treated with increasing doses (n=3/dose) of one of the following modulators of cAMP signaling: epinephrine, salbutamol, forskolin, dbcAMP and rolipram. Fig. 1 shows how each compound modulates cAMP signaling. All 5 of the cAMP signaling modulators tested increased SMN immunostaining in the nucleus as well as in the cytosol of SMA fibroblasts (Fig. 2). Further analysis of SMN localization to gems showed that all 5 of the cAMP signaling modulators increased the number of gems in 100 randomly selected nuclei (Fig. 3A), the proportion of cells containing gems (Fig. 3B) and proportion of cells containing multiple gems (Fig. 3C) in a dose-dependent manner relative to vehicle-treated SMA fibroblasts. While none of the compounds attained gem counts similar to those observed in fibroblasts (GM03814) derived from the mother of GM03813—i.e. carrier fibroblasts, the number of gems/100 nuclei in SMA fibroblasts treated with the highest doses of dbcAMP, forskolin, salbutamol and rolipram reached at least 50% of the gem counts found in carrier fibroblasts.

Development of a Computational Model for the Effect of cAMP Signaling on SMN2 Expression
We developed a computational model of cAMP signaling in humans by modifying a previously published model of the cAMP pathway in yeast [33]. Because of the highly conserved nature of cAMP signaling, essential features of the cAMP pathway are common between humans and yeast and can be modeled with limited changes between species. The original model in yeast consists of 3 ordinary differential equations (ODEs) and 16 parameters [33] (Fig. 4A). By modeling only those functions essential to cAMP and likely conserved between yeast and humans, our base model of the cAMP pathway contained 3 differential equations and 8 parameters (Fig. 4B). Even with this simplified model, we were able to capture the essential dynamics of cAMP signaling reported previously [33] (Fig. 4C). Therefore, our computational model represents an essential set of relationships that are likely at work in humans and clinically relevant.

We then extended this simplified model of cAMP signaling to include production of FL-SMN through CREB and SMN2 (Fig. 5A). We also added
pathways through which treatments to modify cAMP levels may affect FL-SMN production. We used the number of gems/100 nuclei as our experimental dataset—after being converted to concentration ([S1 Table](#))—to determine how well our model fits with observed data. Except for those found in the literature, the parameters between cAMP production and gem formation within the computational model were fit to these experimental data by minimizing the sum of squared error (SSE) between simulation and experiment. After preliminary simulation, select parameters from the base equations were optimized to better capture the dynamics observed in the human system ([Table 1](#)). By comparing model simulations to our experimental data, we can predict which treatments act through the pathways we proposed. The full cAMP:SMN2 model accurately predicted the response of SMA fibroblasts to treatments with forskolin ([Fig. 5B](#)), dbcAMP ([Fig. 5C](#)), and rolipram ([Fig. 5D](#)). Therefore, it is likely that the overall effects of these drugs act through the cAMP signaling cascade as modeled. Both epinephrine ([Fig. 5E](#)) and salbutamol ([Fig. 5F](#)) treatments, however, showed deviations from model predictions. The full cAMP:SMN2 model predicted a nearly linear, dose-dependent increase in gem formation while the data predicted a sharp increase in gem formation followed by a plateau. The data suggest saturation of the G protein-coupled receptors that bind both epinephrine and salbutamol. These compounds may act through additional, cAMP-independent pathways to give their full effect on gem formation or may have additional levels of regulation that were not simulated.

Having built and tested a computational model of FL-SMN production, we next used a local sensitivity analysis to identify which targets in the cAMP signaling pathway may be most beneficial to optimally increase FL-SMN production.

![Fig. 2. The effect of cAMP signaling modulators on SMN localization to gems.](#) SMN immunostaining (red) of GM03813 SMA fibroblasts treated for 5 days with (A) 500 μM dbcAMP, (B) ddH2O (vehicle for A), (C) 100 nM epinephrine, (D) 50 μM forskolin, (E) 100 nM salbutamol, (F) 10 μM rolipram or (G) DMSO (vehicle for C-F). (H) SMN immunostaining of GM03814 carrier fibroblasts. The nuclei were counterstained with Hoescht 33342 (blue). Scale bar, 13 μm.

doi:10.1371/journal.pone.0115473.g002
Fig. 3. The effects of cAMP signaling modulators on gem counts in SMA fibroblasts. GM03813 SMA fibroblasts were treated with differing doses of dbcAMP, epinephrine, forskolin, salbutamol or rolipram for 5 days (n=3/dose/drug). The concentrations for each dose of each drug (in µM) are shown below the appropriate bars of each graph. The vehicle for dbcAMP is ddH2O (black bars) while DMSO (grey) serves as
vehicle for the remaining compounds. The number of SMN-positive nuclear gems was counted in 100 randomly selected nuclei. Gem count analysis was also completed in GM03814 carrier fibroblasts so as to compare the gem data in treated SMA fibroblasts to those observed in healthy cells. The gem count analysis was expressed as (A) the number of gems per 100 nuclei, (B) the proportion of cells containing gems and (C) the proportion of cells containing multiple gems. The asterisk (*) denotes a statistically significant (p<0.05) difference between drug-treated cells and vehicle (either ddH2O for dbcAMP or DMSO for epinephrine, forskolin, salbutamol or rolipram)-treated cells.

doi:10.1371/journal.pone.0115473.g003

**Fig. 4. Development of the simplified cAMP:SMN2 model.** Simplified cAMP model captures essential functions of cAMP signaling. (A) The original cAMP model generated by Williamson et al. [33]. (B) Simplified cAMP model. (C) Predicted concentrations of activated G proteins (GPa; blue lines), activated PKA (PKAa; green lines) and cAMP (red lines) following addition of glucose. The solid lines represent the predictions based on the simplified cAMP model while the dashed lines represent data points obtained from [34, 35].

doi:10.1371/journal.pone.0115473.g004
Fig. 5. Development of the full cAMP:SMN2 model. Final gem concentrations of full cAMP:SMN2 model (A) simulations (open squares) compared to experimental data (closed circles) for varying concentrations of forskolin (B), dbcAMP (C), rolipram (D), epinephrine (E) and salbutamol (F).

doi:10.1371/journal.pone.0115473.g005
production and gem formation. Gem concentrations at steady-state were used as output measures to identify the sensitivities of FL-SMN production to perturbations in each model parameter (Table 2). The Hill coefficient for the binding of phospho-CREB to the CRE present in the SMN2 promoter had the most impact on the final gem concentration in the full cAMP:SMN2 model. Since the Hill coefficient affects the rate of SMN2 transcription, the sensitivity analysis suggests that the transcription of SMN2 has the greater impact on cAMP signaling-induced gem formation and functional, FL-SMN expression.

Using Full cAMP:SMN2 Mathematical Model to Predict the Effects of Combination Treatments on SMN2 Expression

As previously discussed, the full cAMP:SMN2 model accurately predicts the effects of treatment by rolipram, forskolin and dbcAMP. We used the full cAMP:SMN2 model to examine the effect of a simultaneous treatment with two of these three compounds: rolipram + dbcAMP, forskolin + dbcAMP and rolipram + forskolin. All three combinations demonstrated synergistic responses yielding higher steady-state gem concentrations with each increasing dose. However, both combinations with dbcAMP hit a maximum gem concentration around 6.0 pM (Figs. 6A and 6B) while the combination of rolipram and forskolin peaks around 6.7 pM (Fig. 6C). Since the gem concentration in carrier fibroblasts is approximately 7.0 pM (S1 Table), these results suggest that manipulation of the cAMP signaling pathway at multiple points in the cascade can optimally increase SMN2 expression.

### Table 3. Optimized parameter values for cAMP pathway alternate cAMP:SMN2 model.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
<th>Units</th>
<th>Source</th>
</tr>
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<td>GP $k_r$</td>
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<td>(mMmin)^{-1}</td>
<td>This Work</td>
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<tr>
<td>GP $k_r$</td>
<td>G-Protein Deactivation Rate</td>
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</tr>
<tr>
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<td>min^{-1}</td>
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</tr>
<tr>
<td>AC$_{basal}$</td>
<td>Base AC Activation Rate</td>
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<td>V$_m$</td>
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<tr>
<td>K$_m$</td>
<td>PDE Dissociation Rate Constant</td>
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<tr>
<td>T</td>
<td>Transcription Rate</td>
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<td>d$_p$</td>
<td>FL-SMN Degradation Rate Constant</td>
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<td>min^{-1}</td>
<td>[39]</td>
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<td>k$_g$</td>
<td>Gem Formation Rate Constant</td>
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<td>d$_g$</td>
<td>Gem Degradation Rate Constant</td>
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<tr>
<td>F$_{ka}$</td>
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<tr>
<td>$\alpha$</td>
<td>Salbutamol Splicing Constant</td>
<td>5149.72</td>
<td>mM^{-1}</td>
<td>This Work</td>
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The parameters marked with an asterisk (*) were carried over from the simplified cAMP model.

doi:10.1371/journal.pone.0115473.t003
Fig. 6. Simulated treatments of SMA fibroblasts with two different cAMP modulators. Dual dose simulation data for the combination treatments with forskolin and dbcAMP (A), rolipram and dbcAMP (B) and forskolin and rolipram (C).

doi:10.1371/journal.pone.0115473.g006
Development of an Alternate Model for the Effect of cAMP Signaling on \textit{SMN2} Expression

Previous work has shown that activation of PKA directly affects gem formation independent of \textit{SMN2} transcription \cite{39}. Based on this observation, we also developed an alternate model of the interplay between cAMP signaling and the expression of functional FL-SMN and gem formation (the alternate cAMP:SMN2 model; \textbf{Fig. 7A}). We fit the alternate cAMP:SMN2 model to the available gem concentration data (\textit{S1 Table}) as described for the full cAMP:SMN2 model. The downstream parameters as well as select simplified model parameters were included for optimization (\textit{Table 3}). Similar to the full cAMP:SMN2 model, the alternate cAMP:SMN2 model predicted responses due to treatments with forskolin (\textbf{Fig. 7B}), dbcAMP (\textbf{Fig. 7C}) and rolipram (\textbf{Fig. 7D}); the alternate cAMP:SMN2 model also yielded deviations for salbutamol (\textbf{Fig. 7E}) and epinephrine (\textbf{Fig. 7F}) treatments.

With the alternate cAMP:SMN2 model fully optimized, we conducted a normalized local sensitivity analysis in order to reveal the interactions most important for gem production within the alternate pathway. The alternate cAMP:SMN2 model sensitivity results show that both the gem formation and degradation rates have a significant influence on final gem concentration, as would be expected (\textit{Table 4}). Furthermore, their sensitivities are three orders of magnitude greater than the corresponding sensitivity to the Hill coefficient in the full cAMP:SMN2 model. The estimated gem formation rate for the alternate cAMP:SMN2 model is approximately five orders of magnitude larger than that of the full cAMP:SMN2 model, thus making this parameter the key differentiator between the two proposed cAMP:SMN2 models.

We also developed and analyzed a combination model which encompasses the effects of cAMP signaling on the upregulation of \textit{SMN2} promoter activity and transcription (the full cAMP:SMN2 model) as well as the direct stimulation of gem formation by PKA (the alternate cAMP:SMN2 model). The fit of this combination cAMP:SMN2 model to the experimental data, however, was significantly weaker than for the fits of either the full cAMP:SMN2 and alternate cAMP:SMN2 models (data not shown). Therefore, this combinatorial effect of cAMP signaling on the expression of functional \textit{SMN2} is far less likely to be biologically accurate.

\section*{Discussion}

In this study, we use a systems biology approach with mathematical models to characterize the regulation of \textit{SMN2} expression by cAMP signaling. This is the first time, to our knowledge, that a systems biology approach has been used to develop SMA therapeutic strategies. We focused on the interaction between cAMP signaling and \textit{SMN2} expression in this study since there is ample evidence in the literature showing that induction of cAMP signaling increases \textit{SMN2} expression \cite{21–23}. The cAMP signaling treatment data were used to generate two distinct
Fig. 7. Development of the alternate cAMP:SMN2 model. Final gem concentrations of alternate cAMP:SMN2 model (A) simulations (open squares) compared to experimental data (closed circles) for varying concentrations of forskolin (B), dbcAMP (C), rolipram (D), epinephrine (E) and salbutamol (F).

doi:10.1371/journal.pone.0115473.g007
mathematical models—full cAMP:SMN2 and alternate cAMP:SMN2 models—for the interaction of cAMP signaling and SMN2 expression. Simulated data from both models match very well with experimental data suggesting that either model is robust. The mathematical models can also be used to predict the effects of drug combinations on cAMP-mediated regulation of SMN2 expression. This study will also guide future investigations into the mechanisms by which cAMP signaling regulated SMN2 expression.

Gem formation serves as an indicator of the expression of fully functional, FL-SMN protein in this study. Reduced gem formation correlates with SMN protein expression and disease severity in fibroblasts derived from SMA patients [9]. Numerous studies have identified drug compounds that increase the number of gems in SMA patient cells [27, 40–49]. In these studies, drug-induced changes in gem formation are verified by corresponding changes in SMN protein levels in SMA fibroblasts measured by immunoblot or enzyme-linked immunosorbent assays (ELISAs). Some of these gem inducers also increase SMN protein levels in the central nervous system and can ameliorate the phenotype in SMA mouse models [47, 50–52]. These observations support the rationale for using gem formation as an indicator of SMN expression in our mathematical models.

Activation of cAMP signaling increases SMN2 expression but there is debate as to how this signaling cascade regulates SMN2. Some groups report that the regulation of SMN2 promoter activity and mRNA transcription are influenced by cAMP signaling [21–23] but others suggest that the regulation of SMN2 expression by cAMP signaling occurs post-transcriptionally, i.e. by influencing FL-SMN protein stability [39]. The two mathematical models generated in this study for the interaction between cAMP signaling and SMN2 expression—full

<table>
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<td>$d_d$</td>
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<tr>
<td>$K_i$</td>
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</tr>
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<td>PKA $k_i$</td>
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<td>GP $k_r$</td>
<td>$4.06 \times 10^{-7}$</td>
</tr>
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<td>$T$</td>
<td>$3.79 \times 10^{-7}$</td>
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<tr>
<td>K$_{p,PDE}$</td>
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doi:10.1371/journal.pone.0115473.t004
cAMP:SMN2 and alternate cAMP:SMN2 models—differ by whether or not cAMP signaling affects SMN2 transcription. Either model fit very well with the experimental data. However, when the two models were combined, the fit with the experimental data was not strong suggesting that only one model correctly simulates the interaction between the cAMP signaling cascade and SMN2 expression. At present, we cannot determine which mathematical model more accurately simulates cAMP signaling-dependent regulation of SMN2. A detailed examination of the time course of gem formation—as well as other levels of SMN2 regulation—in response to cAMP signaling modulators would permit model discrimination and refinement.

The regulation of SMN expression by cAMP signaling is complex and multifaceted. As a result, some facets of the interaction between cAMP signaling and SMN gene expression were not included in our mathematical models. For example, PKA has been shown to directly phosphorylate SMN in vitro [39,53]. This PKA-dependent phosphorylation of SMN may modulate its interactions with components of the core SMN:gemins macromolecular complex including gemin-2 (SIP1), gemin-5 and gemin-8 [39,53]. Since the effects of PKA phosphorylation of SMN on its function and localization are not yet known, we could not factor this variable in our mathematical models. Also, activation of NMDA-type, glutamatergic receptors increases SMN expression in the spinal cord by AKT-mediated phosphorylation of CREB and repression of ERK-activated Elk-1 [54,55]. It remains to be determined whether cAMP signaling-independent phosphorylation of CREB would affect SMN expression in our model system. Once we have a better understanding of how these events affect SMN expression and function, direct PKA phosphorylation of SMN and the intersection of other signaling pathways—like AKT and MAP kinase (ERK)—can be integrated into mathematical models of the interactions of cAMP signaling on SMN expression and function.

In summary, we have demonstrated that increasing cAMP activation increases FL-SMN production, as measured by gem formation, in human cells using a systems biology approach. We generated data-driven, mathematical models describing the interactions between cAMP signaling and functional FL-SMN production (gem formation) from SMN2. These models can be used to identify the components of the cAMP signaling cascade that may be most effective at increasing SMN levels in SMA cells as well as to predict the effects of combination treatment strategies. Development of cAMP signaling-based therapeutic strategies using a combination of biological data and mathematical modeling will be essential for treating SMA.

Supporting Information

S1 Table. Gems concentrations after treatment with cAMP inducing compounds. doi:10.1371/journal.pone.0115473.s001 (DOCX)
S1 Document. Substitution of Equation 18 into Equation 19 to solve for the PKA term.

doi:10.1371/journal.pone.0115473.s002 (DOCX)

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Author Contributions

Conceived and designed the experiments: SGM DJC PD MERB. Performed the experiments: SGM DJC MERB. Analyzed the data: SGM DJC PD MERB. Contributed reagents/materials/analysis tools: PD MERB. Wrote the paper: SGM DJC PD MERB.

References


